Series JBB/1

SET-1

कोड नं.
Code No. **30/1/1**

रोल नं.
Roll No. ⬚⬚⬚⬚⬚⬚⬚

परीक्षार्थी कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Code on the title page of the answer-book.

नोट	Note
(I) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ 15 हैं।	(I) Please check that this question paper contains **15** printed pages.
(II) कृपया जाँच कर लें कि इस प्रश्न-पत्र में 40 प्रश्न हैं।	(II) Please check that this question paper contains **40** questions.
(III) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए कोड नम्बर को छात्र उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।	(III) Code number given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
(IV) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, प्रश्न का क्रमांक अवश्य लिखें।	(IV) **Please write down the Serial Number of the question in the answer-book before attempting it.**
(V) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक छात्र केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका में कोई उत्तर नहीं लिखेंगे।	(V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.

गणित (मानक) – सैद्धान्तिक

MATHEMATICS (STANDARD) – Theory

निर्धारित समय : *3 घण्टे*
Time allowed : 3 hours

अधिकतम अंक : 80
Maximum marks : 80

General Instructions :

(i) This question paper comprises four sections – A, B, C and D. This question paper carries 40 questions. All questions are compulsory.

(ii) Section A : Q. No. 1 to 20 comprises of 20 questions of one mark each.

(iii) Section B : Q. No. 21 to 26 comprises of 6 questions of two marks each.

(iv) Section C : Q. No. 27 to 34 comprises of 8 questions of three marks each.

(v) Section D : Q. No. 35 to 40 comprises of 6 questions of four marks each.

(vi) There is no overall choice in the question paper. However, an internal choice has been provided in 2 questions of one mark each, 2 questions of two marks each, 3 questions of three marks each and 3 questions of four marks each. You have to **attempt only one of the choices** in such questions.

(vii) In addition to this, separate instructions are given with each section and question, wherever necessary.

(viii) Use of calculators is not permitted.

SECTION - A

Q. No. 1 to 10 are multiple choice type questions of 1 mark each. Select the correct option.

1. If one of the zeroes of the quadratic polynomial $x^2 + 3x + k$ is 2, then the value of k is

   (a) 10 (b) –10 (c) –7 (d) –2

2. The total number of factors of a prime number is

   (a) 1 (b) 0 (c) 2 (d) 3

3. The quadratic polynomial, the sum of whose zeroes is –5 and their product is 6, is

   (a) $x^2 + 5x + 6$ (b) $x^2 - 5x + 6$ (c) $x^2 - 5x - 6$ (d) $-x^2 + 5x + 6$

4. The value of k for which the system of equations $x + y - 4 = 0$ and $2x + ky = 3$, has no solution, is

   (a) –2 (b) ≠2 (c) 3 (d) 2

5. The HCF and the LCM of 12, 21, 15 respectively are

    (a) 3, 140   (b) 12, 420   (c) 3, 420   (d) 420, 3

6. The value of x for which $2x, (x+10)$ and $(3x+2)$ are the three consecutive terms of an AP, is

    (a) 6   (b) −6   (c) 18   (d) −18

7. The first term of an AP is p and the common difference is q, then its 10th term is

    (a) $q+9p$ (b) $p-9q$ (c) $p+9q$ (d) $2p+9q$

8. The distance between the points $(a \cos \theta + b \sin \theta, 0)$ and $(0, a \sin \theta - b \cos \theta)$, is

    (a) a^2+b^2 (b) a^2-b^2 (c) $\sqrt{a^2+b^2}$ (d) $\sqrt{a^2-b^2}$

9. If the point $P(k, 0)$ divides the line segment joining the points $A(2, -2)$ and $B(-7, 4)$ in the ratio $1 : 2$, then the value of k is

    (a) 1   (b) 2   (c) −2   (d) −1

10. The value of p, for which the points $A(3,1)$, $B(5, p)$ and $C(7, -5)$ are collinear, is

    (a) −2   (b) 2   (c) −1   (d) 1

In Q. Nos. 11 to 15, fill in the blanks. Each question is of 1 mark.

11. In Fig. 1, Δ ABC is circumscribing a circle, the length of BC is _____ cm.

Fig. 1
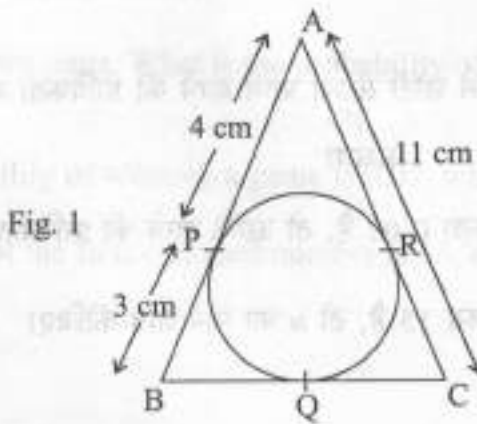
12. Given $\triangle ABC \sim \triangle PQR$, if $\dfrac{AB}{PQ} = \dfrac{1}{3}$, then $\dfrac{ar(\triangle ABC)}{ar(\triangle PQR)} = $ _____.

13. ABC is an equilateral triangle of side $2a$, then length of one of its altitude is _____.

14. $\dfrac{\cos 80°}{\sin 10°} + \cos 59° \operatorname{cosec} 31° = $ _____.

15. The value of $\left(\sin^2 \theta + \dfrac{1}{1 + \tan^2 \theta} \right) = $ _____.

Or

The value of $(1 + \tan^2 \theta)(1 - \sin \theta)(1 + \sin \theta) = $ _____.

Q. Nos. 16 to 20 are short answer type questions of 1 mark each.

16. The ratio of the length of a vertical rod and the length of its shadow is $1 : \sqrt{3}$. Find the angle of elevation of the sun at that moment?

17. Two cones have their heights in the ratio 1:3 and radii in the ratio 3:1. What is the ratio of their volumes?

18. A letter of English alphabet is chosen at random. What is the probability that the chosen letter is a consonant.

19. A die is thrown once. What is the probability of getting a number less than 3?

Or

If the probability of winning a game is 0.07, what is the probability of losing it?

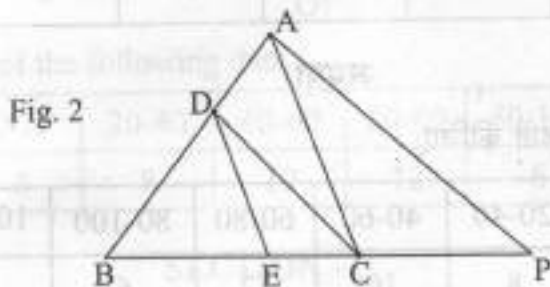20. If the mean of the first n natural number is 15, then find n.
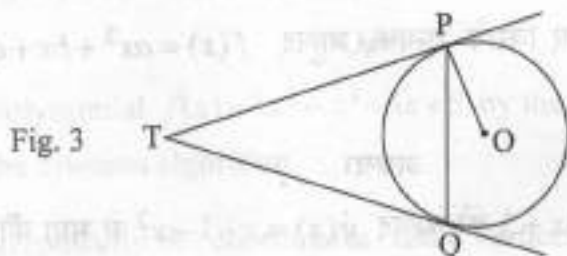
SECTION - B

Q. Nos. 21 to 26 carry 2 marks each.

21. Show that $(a-b)^2, (a^2+b^2)$ and $(a+b)^2$ are in AP.

22. In Fig. 2, DE ∥ AC and DC ∥ AP. Prove that $\dfrac{BE}{EC} = \dfrac{BC}{CP}$.
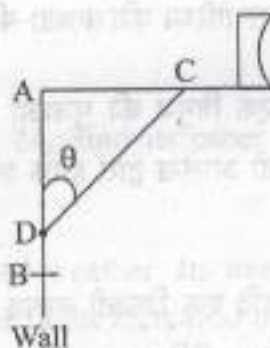

Fig. 2

Or

In Fig. 3, two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2 \angle OPQ$.

Fig. 3

23. The rod AC of a TV disc antenna is fixed at right angles to the wall AB and a rod CD is supporting the disc as shown in Fig. 4. If AC = 1.5 m long and CD = 3 m, find (i) tan θ (ii) sec θ + cosec θ

Fig. 4

24. A piece of wire 22 cm long is bent into the form of an arc of a circle subtending an angle of 60° at its centre. Find the radius of the circle. $\left[\text{Use } \pi = \dfrac{22}{7}\right]$

25. If a number x is chosen at random from the numbers $-3, -2, -1, 0, 1, 2, 3$. What is probability that $x^2 \leq 4$?

26. Find the mean of the following distribution :

Class :	3-5	5-7	7-9	9-11	11-13
Frequency :	5	10	10	7	8

Or

Find the mode of the following data :

Class :	0-20	20-40	40-60	60-80	80-100	100-120	120-140
Frequency	6	8	10	12	6	5	3

SECTION - C

Q. Nos. 27 to 34 carry 3 marks each.

27. Find a quadratic polynomial whose zeroes are reciprocals of the zeroes of the polynomial $f(x) = ax^2 + bx + c, a \neq 0, c \neq 0$.

Or

Divide the polynomial $f(x) = 3x^2 - x^3 - 3x + 5$ by the polynomial $g(x) = x - 1 - x^2$ and verify the division algorithm.

28. Determine graphically the coordinates of the vertices of a triangle, the equations of whose sides are given by $2y - x = 8$, $5y - x = 14$ and $y - 2x = 1$.

Or

If 4 is a zero of the cubic polynomial $x^3 - 3x^2 - 10x + 24$, find its other two zeroes.

29. In a flight of 600 km, an aircraft was slowed due to bad weather. Its average speed for the trip was reduced by 200 km/hr and time of flight increased by 30 minutes. Find the original duration of flight.
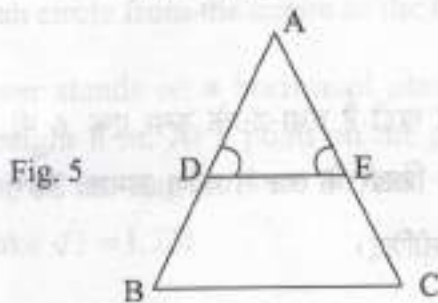
30. Find the area of triangle PQR formed by the points $P(-5, 7), Q(-4, -5)$ and $R(4, 5)$.

Or

If the point $C(-1, 2)$ divides internally the line segment joining $A(2, 5)$ and $B(x, y)$ in the ratio 3:4, find the coordinates of B.

31. In Fig. 5, $\angle D = \angle E$ and $\dfrac{AD}{DB} = \dfrac{AE}{EC}$, prove that BAC is an isosceles triangle.

Fig. 5

32. In a triangle, if square of one side is equal to the sum of the squares of the other two sides, then prove that the angle opposite to the first side is a right angle.

33. If $\sin \theta + \cos \theta = \sqrt{3}$, then prove that $\tan \theta + \cot \theta = 1$.

34. A cone of base radius 4 cm is divided into two parts by drawing a plane through the mid-point of its height and parallel to its base. Compare the volume of the two parts.

SECTION - D

Q. Nos. 35 to 40 carry 4 marks each.

35. Show that the square of any positive integer cannot be of the form $(5q + 2)$ or $(5q + 3)$ for any integer q.

Or

Prove that one of every three consecutive positive integers is divisible by 3.

36. The sum of four consecutive numbers in AP is 32 and the ratio of the product of the first and last terms to the product of two middle terms is 7:15. Find the numbers.

Or

Solve : $1 + 4 + 7 + 10 + \ldots + x = 287$

37. Draw a line segment AB of length 7 cm. Taking A as centre, draw a circle of radius 3 cm and taking B as centre, draw another circle of radius 2 cm. Construct tangents to each circle from the centre of the other circle.

38. A vertical tower stands on a horizontal plane and is surmounted by a vertical flag-staff of height 6 m. At a point on the plane, the angle of elevation of the bottom and top of the flag-staff are $30°$ and $45°$ respectively. Find the height of the tower. (Take $\sqrt{3} = 1.73$)

39. A bucket in the form of a frustum of a cone of height 30 cm with radii of its lower and upper ends as 10 cm and 20 cm, respectively. Find the capacity of the bucket. Also find the cost of milk which can completely fill the bucket at the rate of Rs. 40 per litre. $\left(\text{Use } \pi = \dfrac{22}{7}\right)$

40. The following table gives production yield per hectare (in quintals) of wheat of 100 farms of a village :

Production yield/hect.	40-45	45-50	50-55	55-60	60-65	65-70
No. of farms	4	6	16	20	30	24

Change the distribution to 'a more than' type distribution and draw its ogive.

Or

The median of the following data is 525. Find the values of x and y, if total frequency is 100 :

Class :	0-100	100-200	200-300	300-400	400-500	500-600	600-700	700-800	800-900	900-1000
Frequency :	2	5	x	12	17	20	y	9	7	4